

# A 0.5V 3<sup>rd</sup>-order Tunable $g_m$ -C Filter

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**Abstract.** This paper proposes a 3<sup>rd</sup>-order  $g_m$ -C filter that operates with the extremely low voltage supply of 0.5 V. The employed transconductor is capable for operating in an extremely low voltage power supply environment. A benefit offered by the employed transconductor is that the filter's cut-off frequency can be tuned, through a dc control current, for relatively large ranges. The filter structure was designed using normal threshold transistors of a triple-well 0.13 $\mu$ m CMOS process and is operated under a 0.5V supply voltage; its behavior has been evaluated through simulation results by utilizing the Analog Design Environment of the Cadence software.

## Keywords

$G_m$ -C filters, analog filters, low voltage circuits.

## 1. Introduction

The operational transconductance amplifiers or  $g_m$  stages are used in the constructions of a number of continuous time circuits for analog signal processing such as filters and oscillators [1], [2]. The most often implementations of continuous-time filters are based on the  $g_m$ -C approach. A transconductor stage normally does not need frequency compensation as the operational amplifier does in order to ensure its stability and therefore it does not include low frequency poles. The advantage of  $g_m$ -C based continuous-time filters compared with active-RC filters is the higher frequency performance. Even if the transistors of the basic blocks operate in weak inversion and they cannot achieve the high frequency of the strong inversion operating transistors, they still keep advantage comparing with other topologies in terms of power consumption per pole. In addition, the resulted topologies are resistorless due to the employment of the small-signal transconductance parameters of the  $g_m$  stages, giving the potential for performing electronic adjustment of their frequency characteristics. On the other hand, the linear performance is worsened due to the restriction for operation in small-signal conditions.

The conventional transconductor stage uses a simple differential MOS transistor pair where its transconductance is easily controlled by modifying the tail current. A very interesting  $g_m$  stage topology is based on CMOS inverter and is called Nauta's transconductor. This transconductor is a very robust building block for implementing high fre-

quency  $g_m$ -C filters [3], [4] because it does not include internal nodes and therefore low frequency poles. The Nauta's transconductor is based on six CMOS inverters in differential mode configuration. Due to the topology simplicity this block can operate in lower voltage supply comparing with conventional transconductors. However, based on this concept several CMOS inverter-based transconductors have been published [5-8] proposing transconductance control methodologies in order to use them as basic devices in tunable filters. To achieve tunable transconductance, the supply nodes of the internal inverters must be independent from the main chip supply [2], [3]. Therefore, tunable voltage regulators are used which are stacked on the CMOS inverters excluding this transconductor from low-voltage applications. Some alternative tuning concepts have been reported, using the input common-mode (CM) voltage [5] or floating-gate MOS (FGMOS) transistors [6].

In this paper we used a modified Nauta's current-controlled  $g_m$  stage, by means of transconductance tuning, in the construction of extremely low voltage continuous time  $g_m$ -C filters. Despite of operating the MOS devices in the weak inversion, the  $g_m$  stage is able to support filter applications in the range of few MHz due to the absence of internal nodes. The bulk voltages of the devices which are included in the  $g_m$  stage are appropriately modified through a control circuit achieving a linearly current-controlled transconductance [9]. The cut-off frequency of the filter can be easily adjusted through a control current using 0.5V voltage supply and offering also high  $g_m/I_{DD}$  ratio and circuit simplicity. All circuitries were designed using a triple-well 0.13 $\mu$ m CMOS process.

The paper is organized as follows: in Section 2 the filter topology is described. In Section 3, the simulation results verify the circuit operation and the performance comparing with other low-voltage topologies is given.

## 2. Filter Description

The topology of the LC ladder passive prototype filter is shown in Fig. 1(a), where its element values for realizing the normalized 3<sup>rd</sup>-order Butterworth filter function in (1)

$$H(s) = \frac{1}{s^3 + 2s^2 + 2s + 1} \quad (1)$$

are  $C_{1p} = C_{3p} = 1$  F,  $L_{2p} = 2$  H, and  $R_S = R_L = 1$   $\Omega$ .

Following the leapfrog technique, the derived active  $g_m$ -C filter topology is depicted in Fig. 1(b).

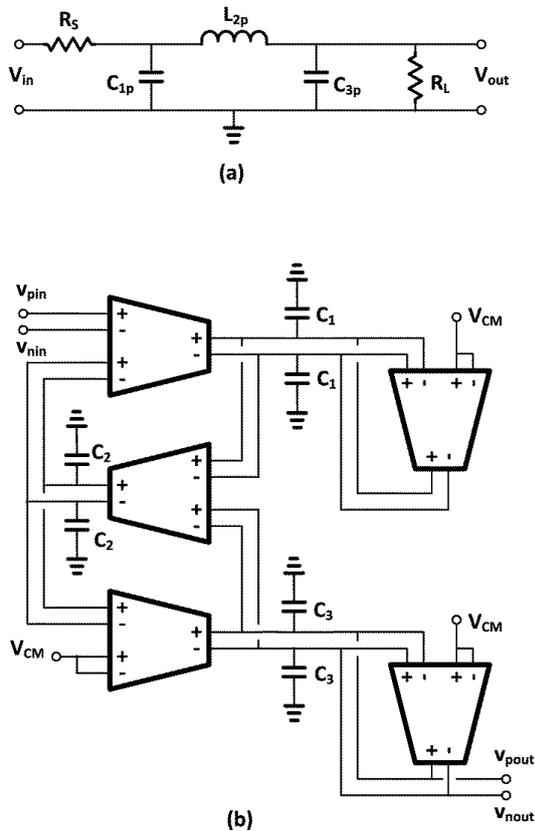


Fig. 1. Filter topology: a) passive prototype/circuit and b) active implementation.

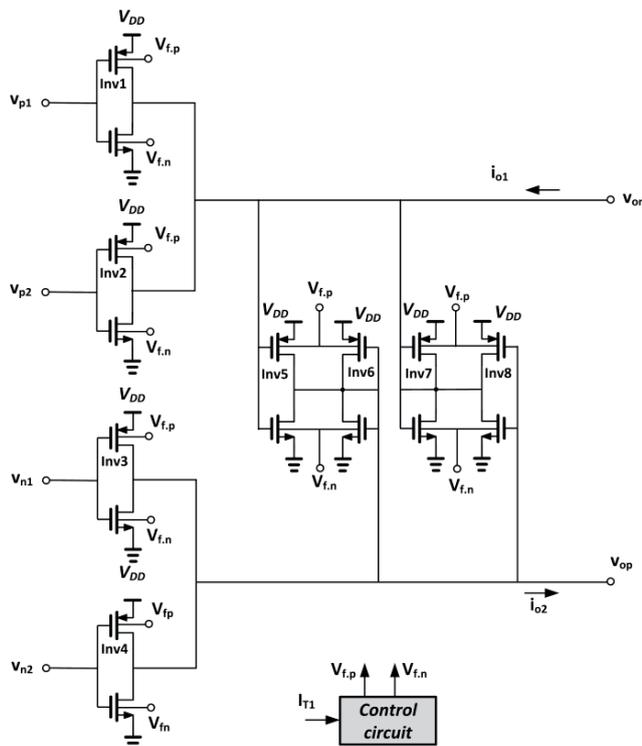


Fig. 2. The double input differential  $g_m$  stage.

The core of the filter is the differential double input  $g_m$  stage with two very important features: the capability for operation with an extremely low-voltage power supply and the linearly current-controlled transconductance. The circuit of the  $g_m$  stage, which is based on the  $g_m$  stage proposed in [9], is shown in Fig. 2. In this paper, the transconductor has been modified in order to create multiple inputs suitable to be employed in the filter of Fig. 1.

In order to achieve both, low-voltage operation and transconductance tuning, the bulk terminals of the transistors are not connected to constant voltages as in conventional circuit topologies, but they are used to adjust their bias. Inverters Inv1 to Inv4 form the double input differential transconductor, inverters Inv5, Inv8 form the differential output load and inverters Inv6, Inv7 form the common mode (CM) output load. All inverters are controlled through the bulk voltages  $V_{fp}$  and  $V_{fn}$  which are generated by the Control circuit and the control current  $I_{T1}$ .

The transconductance controlled methodology is based on the master-slave technique using the control circuit which is shown in Fig. 3a. The CMOS inverter which is formed by  $M_{p,s}$  and  $M_{n,s}$ , is the slave or active transconductor element and the input voltage  $V_{in}$  is applied at its input assuming also that input CM equal to middle supply ( $V_{DD}/2$ ). The bulk terminals of both transistors are adjusted by the control circuit generating the voltages  $V_{fp}$  and  $V_{fn}$  which appropriately adjusted, bias the inverter with the desired quiescent current. Transistors  $M_{p,m}$ - $M_{n,m}$  and  $M_{p,s}$ - $M_{n,s}$  are the master the slave devices, respectively. The aspect ratios of the master devices are scaled down  $m$  times compared with the corresponding slave devices to minimize the area and current consumption. Therefore, the quiescent current of the slave devices are  $m$  times larger ( $mI_T$ ) than those of the master devices ( $I_T$ ).

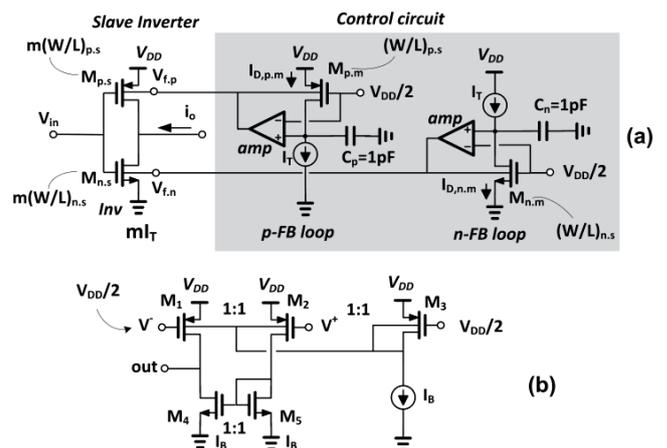


Fig. 3. (a) Schematic diagram of the proposed technique and (b) the circuit of the differential amplifier (amp).

The feedback voltages  $V_{fp}$  and  $V_{fn}$  are applied to the bulk terminal of the  $M_{p,s}$  and  $M_{n,s}$ , respectively, of the slave inverter. Therefore, the quiescent current of the slave inverter will be  $mI_T$  and the output CM voltage will be  $V_{DD}/2$ . Eventually, using this approach the transconductances  $g_{m,p,s}$  and  $g_{m,n,s}$  of  $M_{p,s}$  and  $M_{n,s}$ , respectively, can be

adjusted by means of the controlling current  $I_T$ . The feedback loops ensure also, that the output CM voltage is kept constant, equal to  $V_{DD}/2$  and independent from the value of  $I_T$ .

According to the above considerations and assuming that all transistors operate in weak-inversion [8] the transconductance of the slave inverter will be equal to,

$$g_{m,s} = g_{m,p,s} + g_{m,n,s} = (I_{D,p,s} + I_{D,n,s})/nV_t = 2mI_T/nV_t \quad (2)$$

where  $g_{m,p,s}$ ,  $g_{m,n,s}$  are the transconductance and  $I_{D,p,s}$ ,  $I_{D,n,s}$  are the drain current of the  $M_{p,s}$  and  $M_{n,s}$  transistors, respectively, shown in Fig. 3a. Also,  $n$  is the slope factor and  $V_t = kT/q$  is the thermal voltage.

The output current of the transconductor in Fig. 2 is,

$$i_{dif} = i_{o1} - i_{o2} = v_{in,dif} g_{m,d} = (v_{p1} - v_{n1} + v_{p2} - v_{n2})g_{m,s} \quad (3)$$

The circuit of the differential amplifier which is employed in FB loops is shown in Fig. 3b. The input differential pair is formed by the pMOS devices  $M_1$ ,  $M_2$ . Transistor  $M_3$  is biased by the constant current  $I_B$ . Based on Figs. 3a and 3b, the constant voltage of  $V_{DD}/2$  is applied to the gate voltage of  $M_1$  and the feedback loops ensure that the gate voltage of  $M_2$  will be locked at  $V_{DD}/2$ . Therefore, transistors  $M_1$ ,  $M_2$  and  $M_3$  act, actually, as current mirror for CM signals and the quiescent drain currents of  $M_1$ ,  $M_2$  will be equal to  $I_B$ .

### 3. Simulation and Comparison Results

To verify the operation of the proposed filter, the circuit was designed and simulated using a triple well 0.13 $\mu$ m CMOS process with  $V_{DD} = 0.5$  V. The transistors used in the simulations have a normal threshold voltage. The 3<sup>rd</sup> order Butterworth filter of Fig. 1b has a nominal cutoff frequency equal to 1 MHz for  $I_{T1}$  10  $\mu$ A. The capacitors of the filter have values  $C_1 = C_3 = 74.31$  pF and  $C_2 = 148.63$  pF.

The transistors' aspect ratios of the transconductor in Fig. 3 were  $(W/L)_{p,s1,2} = 100 \mu\text{m}/0.5 \mu\text{m}$ ,  $(W/L)_{n,s1,2} = 50 \mu\text{m}/0.5 \mu\text{m}$  for  $I_{nv1,2}$ ,  $(W/L)_{p,s3-6} = 25 \mu\text{m}/0.5 \mu\text{m}$ ,  $(W/L)_{n,s3-6} = 12.5 \mu\text{m}/0.5 \mu\text{m}$  for  $Inv3-6$  and  $(W/L)_{1-3} = 10 \mu\text{m}/0.5 \mu\text{m}$ ,  $(W/L)_{4,5} = 30 \mu\text{m}/0.5 \mu\text{m}$  for the amplifier.

The scale factor was  $m = 4$  and the bias current of  $I_B = 1 \mu\text{A}$ . The transconductance  $g_m$  and the gain-bandwidth product GBW of the transconductor are illustrated as functions of the tuning current  $I_{T1}$  in Fig. 4 [9]. THD is -40 dB for an input signal with amplitude 50 mV. Also, it is important that the common mode output is almost constant from process and temperature variations due to the internal feedback loop.

The cutoff frequency as function of the tuning current  $I_{T1}$  is plotted in Fig. 5. The lowest and highest cutoff frequency is 0.94 MHz and 5.1 MHz, for  $I_{T1}$  current 10  $\mu$ A and 80  $\mu$ A, respectively. In Fig. 6 the frequency responses are depicted for  $I_{T1}$  ranging between 10  $\mu$ A and 80  $\mu$ A. From Fig. 5 and Fig. 6 it becomes obvious that the relation

between cutoff frequency and control current  $I_{T1}$  is not completely linear as expected from (2). This can be explained by the fact that the tuning range has been realized using a relatively high drain current variation. Increasing the drain current of a MOS transistor the drain-source conductance is decreased affecting the accuracy of (3).

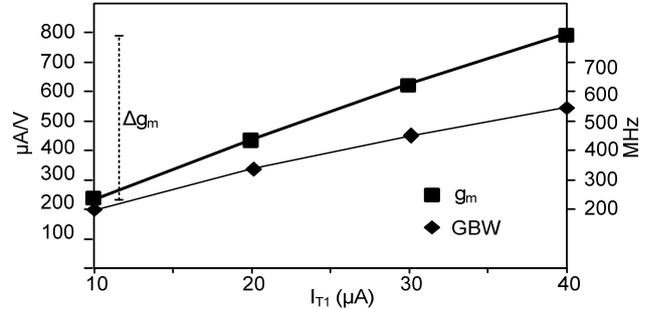


Fig. 4. Input transconductance  $g_m$  as function of  $I_{T1}$ .

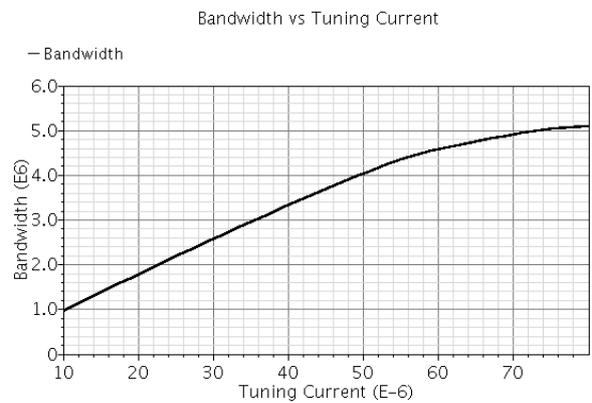


Fig. 5. Cutoff frequency as function of  $I_{T1}$ .

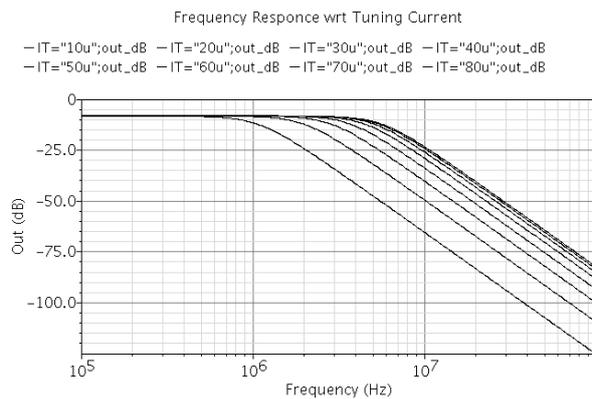


Fig. 6. Frequency responses for a range of  $I_{T1}$  from 10  $\mu$ A to 80  $\mu$ A.

Monte Carlo simulations have been performed in order to inspect the influence of the process and mismatch variations on the cutoff frequency of the filter. The results are shown in Fig. 7. The mean value is at 0.97 MHz with a standard deviation  $\sigma = 17.4$  kHz, corresponding to 1.7% deviation from the nominal value. Also, corner analysis simulation results are summarized in Tab. 1. For the results the current  $I_{T1}$  is 10  $\mu$ A,  $V_{DD}$  is 0.5 V and input amplitude

51.75 mV. As expected, while most of the parameters are unaffected, however there is a significant influence in the cutoff frequency, mostly due to the capacitor variations. It is known that the fully integrated filters may deviate from the nominal frequency with the corner variations, and therefore an automatic tuning topology is required when the accuracy is of high importance. The proposed filter is suitable to be combined with automatic frequency tuning technique, due to its inherent ability for electronic tuning.

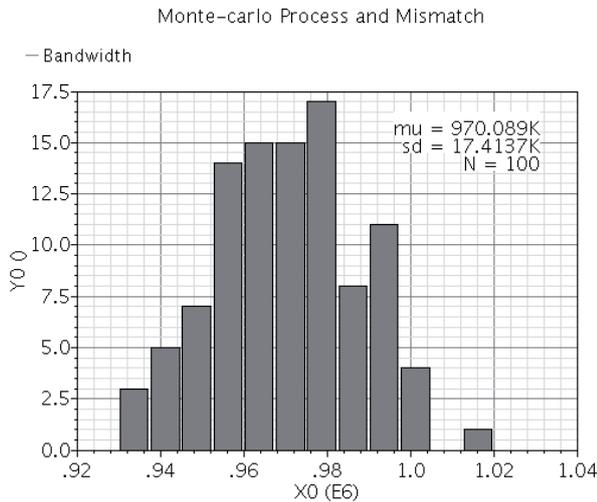


Fig. 7. Monte Carlo simulation results for the filter cutoff frequency.

In Tab. 2 the performance of the filter and some of its parameters are compared with other implementations of  $g_m$ -C filters [9]-[13]. This filter has the lowest supply voltage and also shows the best power consumption. Also, the values of other parameters of the filter, including dynamic range, noise, operating frequency and tuning range are comparable with the values of the other filters. The final conclusion is that this filter can achieve almost similar performance with other topologies but with significant reduction in supply voltage and in power consumption

which is extremely important in mobile and biomedical applications. Some parameters of this filter may be worse, such as the tuning range. However, this is the price paid for operating in ultra low supply voltage using transistors of typical threshold.

	Unit	Typical	Fast-best	Slow-worst
Temperature	°C	27	-25	80
Cutoff frequency	MHz	0.970	1.165	0.819
Power Consumption @ $I_{T1} = 10 \mu A$	$\mu W$	-339.2	-328.5	-338.7
Consumption Current	$\mu A$	-678.4	-657.0	-677.5
DC differential gain	dB	-8.1	-8.6	-7.4
CMRR	dB	-31.3	-31.0	-31.5
Dynamic Range		63.13	65.44	60.49
Integrated Noise (1 kHz-1 MHz)	$\mu V_{rms}$	9.4	7.0	12.8
Input Referred Noise (1 kHz - 1 MHz)	$\mu V_{rms}$	25.5	19.5	34.6
Input Referred Noise (Spot Noise@1 kHz)	nV/ $\sqrt{Hz}$	217.51	193.12	242.85
Input Referred Noise (Spot Noise@1 MHz)	nV/ $\sqrt{Hz}$	27.56	16.75	46.44
DC Output Voltage	mV	249.9	249.7	251.4
Input Offset	mV	-0.06	-0.331	1.359

Tab. 1. Parameter values of the filter vs corner variations.

### 4. Conclusion

A low-voltage filter operating at 0.5 V is proposed in this paper. The filter is constructed from transconductors based on simple inverters, where their transconductance is controlled by the bulk voltage. The tuning range of the filter is controllable by a single control current. The filter has been simulated using transistor models with normal threshold voltage of a 0.13 $\mu m$  CMOS technology. The topology shows low power consumption and good performance in terms of noise, linearity, tunability and dynamic range.

	Unit	This Filter	[11]	[12]	[13]	[14]	[15]
Process		0.13 $\mu m$ CMOS	0.35 $\mu m$ CMOS	0.35 $\mu m$ CMOS	0.18 $\mu m$ CMOS	0.18 $\mu m$ CMOS	0.35 $\mu m$ CMOS
Supply/VDD	V	0.5	1.1	1.2	1.8	1	2.7
Filter Order		3	2	2	4	3	4
Bandwidth	MHz	0.9705	2.66	3			2.5
Frequency /Tuning range	MHz	0.97 - 5.1	0.05 - 2.6		0.5 - 12	0.135 - 2.2	0.2 - 2.5
Linearity/ THD		THD -40 dB @ 51.75 mVpp	THD -38 dB (0.4 Vp-p@ 2.6 MHz)	THD -40 dB @ 1.8 Vp-p		IM3 < 68.5 dB @ 2 MHz	Linearity 1 dB Comp 620 mVp-p diff
Power Consumption	$\mu W$	332	720	382	1100-4700	2000	1674
Spot noise	nV/ $\sqrt{Hz}$ @1MHz	27.56				65	41
Integrated noise	$\mu V_{rms}$	9.44#		210 *			
Dynamic Range	dB	63.13		69.6			
Bulk/Gate Driven		Bulk Driven	Gate Driven	Bulk Driven	Gate Driven	Gate Driven	Gate Driven
Applications		Bluetooth	GSM, UMTS, WCDMA	2nd order FD OTA-C low pass filter	IEEE802.11 W-LANs, W-CDM, Bluetooth	GSM, Bluetooth, cdma2000, wide-band CDMA	GSM, IS-95, UMTS

\*Integrated input referred Noise (100 Hz - 4 MHz)

#Total Summarized Noise (Output Noise 1 kHz-1 MHz)

Tab. 2. Comparison with other filter topologies.

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## References

- [1] TSIVIDIS, Y., BANU, M. KHOURY J. Continuous-time MOSFET-C filters in VLSI. *IEEE Journal of Solid-State Circuits*, 1986, vol. 21, no. 1, p.15–30.
- [2] RODRIGUES-VASQUEZ, A., LINARES-BARRANCO, B., HUERTAS, J. SANCHEZ-SINENSIO, E. On the design of voltage controlled sinusoidal oscillators using OTA's. *IEEE Trans. Circuit and Systems*, 1990, vol. 37, no. 2, p. 198-211.
- [3] NAUTA, B. A CMOS transconductance-C filter technique for very high frequencies. *IEEE Journal of Solid-State Circuits*, 1992, vol. 27, no. 2, p. 142 - 153.
- [4] ANDREANI, P., MATTISSON, S. On the use of Nauta's trans-conductor in low-frequency CMOS  $g_m$ -C bandpass filters. *IEEE Journal of Solid-State Circuits*, 2002, vol. 37, no. 2, p. 114 -124.
- [5] LEE, T., PAN, H. A low-voltage CMOS transconductor for VHF continuous-time filters. In *Proceedings of the IEEE International Symposium on Circuits and Systems (ISCAS)*. Hong Kong, 1997, p. 213 - 216.
- [6] MUÑOZ, F., TORRALBA, A., CARVAJAL, R. G., TOMBS, J., RAMIREZ-ANGULO, J. Floating-gate-based tunable low-voltage linear transconductor and its application to HF gm-C filters design. *IEEE Transactions on Circuits and Systems-II*, 2001, vol. 48, no. 1, p. 106 - 110.
- [7] SUADET, A., KASEMSUWAN, V. A CMOS inverter-based class-AB pseudo differential amplifier for HF applications. In *Proc. of the IEEE International Conf. of Electron Devices and Solid-State Circuits (EDSSC)*. Hong Kong (China), 2010, p. 1 - 4.
- [8] BARTHELEMY, H., MEILLERE, S., GAUBERT, J., DAHAESE, N., BOURDEL, S. OTA based on CMOS inverters and application in the design of tunable bandpass filter. *Analog Integrated Circuits and Signal Processing*, 2008, vol. 57, no. 3, p. 169 - 178.
- [9] VLASSIS, S. 0.5 V CMOS inverter-based tunable transconductor. *Analog Integrated Circuits and Signal Processing*, 2012, vol. 72, no. 1, p. 289 - 292.
- [10] VITTOZ, E. Weak inversion in analog and digital circuits. In *System Level Implications on Circuit Design Workshop (CCCD)*, 2003, Lund (Sweden).
- [11] SANTHANALAKSHMI, M., VANATHI, P. T. An improved OTA for a 2<sup>nd</sup> order  $g_m$ -C low pass filter. *European Journal of Scientific Research*, 2011, vol. 66, no.1, p. 75 - 84.
- [12] CARILLO, J. M., DOMINGUEZ, M. A., DUQUE-CARRILLO, J. F. 1.2V fully differential OTA-C lowpass filter based on bulk-driven MOS transistors. In *Proc. of the 20<sup>th</sup> European Conf. on Circuit Theory and Design (ECCTD)*. Linköping (Sweden), 2011.
- [13] HORI, S., MAEDA, T., MATSUNO, N., HIDA, H. Low-power widely tunable  $g_m$ -C filter with an adaptive DC-blocking, triode-biased MOSFET transconductor. In *Proceeding of the 30th European Solid-State Circuits Conference (ESSCIRC)*. Leuven, (Belgium), 2004, p. 99 - 102.
- [14] LO, T. Y., HUNG, C. C. Multi-mode Gm-C channel selections filter for mobile applications in 1V supply voltage. *IEEE Transactions on Circuits and Systems-II: Express briefs*, 2008, vol. 55, no. 4, p. 314 - 318.
- [15] STEHR, U., HENKEL, F., DALLIGE, L., WALDOW, P. A fully differential CMOS integrated 4<sup>th</sup> order reconfigurable GM-C low pass filter for mobile communication. In *Proceeding of the 11<sup>th</sup>*

*IEEE International Conference on Circuits and Systems (ICECS)*. Tel Aviv (Israel), 2003, vol. 1, p. 144-147.

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